

## Constraints and Updating

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Section 7: Constraints and Updating

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## Constraints

Constraints express the integrity rules for a database.

Enforcement of constraints by the DBMS ensures that the database is at all times in a *consistent* state.

A constraint is a *truth-valued* expression, such as a *comparison*, declared as part of the *logical schema* of the database.

The comparands of a constraint are typically relation expressions or invocations of aggregate operators.

But the commonest kinds of constraint are expressed using special shorthands, like KEY, FOREIGN KEY, IS\_EMPTY.

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## KEY Constraints

The constraint shown below is a “uniqueness” constraint, meaning that no two distinct tuples can match on both StudentId and CourseId.

{ StudentId, CourseId } is a *superkey* of EXAM\_MARK

(( EXAM\_MARK GROUP { Mark } AS Marks  
WHERE COUNT ( Marks ) > 1 ) { } ) = RELATION { } { }

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## When a Superkey Is a Key

If no proper subset of superkey  $K$  is a superkey, then  $K$  is a *key*.

So { StudentId, CourseId } is in fact a key of EXAM\_MARK, and is in fact the only key of EXAM\_MARK.

In general a relvar can have several keys, in which case it is sometimes useful to nominate one of them as being the *primary key*. For that reason, keys are sometimes referred to as *candidate keys*. When a primary key is nominated, any other keys are called *alternate keys*.

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## The KEY Shorthand

Traditionally, a KEY constraint is declared as part of the definition of the relvar to which it pertains, thus:

```
VAR EXAM_MARK BASE RELATION {  
  StudentId SID,  
  CourseId CID,  
  Mark INTEGER }  
KEY { StudentId, CourseId } ;
```

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## Multiple Keys

Recall PLUS ( $a + b = c$ ):

a	b	c
1	2	3
2	3	5
2	1	3

Not a variable, of course, but we can still observe that {a, b}, {a, c} and {b, c} are all keys. We might even nominate {a, b} to be the primary key (for psychological reasons only).

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## Degenerate Cases of Keys

The entire heading can be a key. In that case it is the only key (why?).

The empty set can be a key. In that case it is the only key (why?). What special property is implied by such a key?

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## “Foreign Key” Constraints

### IS\_CALLED

StudentId	Name
S1	Anne
S2	Boris
S3	Cindy
S4	Devinder
S5	Boris

### KEY { StudentId }

### IS\_ENROLLED\_ON

StudentId	CourseId
S1	C1
S1	C2
S2	C1
S3	C3
S4	C1

Every StudentId value here must also appear in IS\_CALLED { StudentId }

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## Inclusion Dependency

FOREIGN KEY { StudentId } REFERENCING IS\_CALLED included in declaration of IS\_ENROLLED\_ON is shorthand for:

IS\_CALLED { StudentId }  $\supseteq$  IS\_ENROLLED\_ON { StudentId }

Such constraints in general are sometimes called *inclusion dependencies*. An inclusion dependency is a foreign key if the heading common to the two comparands is a key of the referenced relvar.

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## A Special Case of Inclusion Dependency

Consider:

TABLE\_DUM  $\supseteq r \{ \}$   
 $\equiv$  RELATION { } { }  $\supseteq r \{ \}$

In **Tutorial D** we can write this as **IS\_EMPTY ( r )**.

Also:

$r1 \supseteq r2 \equiv$  IS\_EMPTY (  $r2 \text{ MINUS } r1$  )  
 $\uparrow$   
 $\equiv r2 \text{ NOT MATCHING } r1$

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## IS\_EMPTY Example

### EXAM\_MARK

This might be subject to the constraint:  
 $0 \leq \text{Mark} \leq 100$

**IS\_EMPTY (**  
 $\text{EXAM_MARK WHERE}$   
 $\text{Mark} < 0 \text{ OR } \text{Mark} > 100$  **)**

StudentId	CourseId	Mark
S1	C1	85
S1	C2	49
S2	C1	49
S3	C3	66
S4	C1	93

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## Generalisation of Inclusion Dependency

**IS\_EMPTY ( r1 NOT MATCHING r2 )**

E.g., to express that foreign key in IS\_ENROLLED\_ON:

**IS\_EMPTY ( IS\_ENROLLED\_ON**  
 $\text{NOT MATCHING IS_CALLED } )$

But now the operands can be arbitrary relation expressions, without the restrictions of FOREIGN KEY.

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## “Exclusion Dependency”?

**IS\_EMPTY ( *r1* MATCHING *r2* )**

E.g., to enforce disjointness of part-time and full-time employees:

**IS\_EMPTY ( PART\_TIMER MATCHING FULL\_TIMER )**

Equivalently:

**IS\_EMPTY ( FULL\_TIMER MATCHING PART\_TIMER )**

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## Constraint Declaration

In **Tutorial D** (in addition to KEY specifications written inside relvar declarations):

**CONSTRAINT *name* *expression* ;**

E.g.: **CONSTRAINT Marks\_out\_of\_100 IS\_EMPTY ( EXAM\_MARK WHERE Mark < 0 OR Mark > 100 ) ;**

And to cancel this constraint:

**DROP CONSTRAINT Marks\_out\_of\_100 ;**

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## Relational Update Operators

In theory, only assignment is needed. For example, to enrol student S5 on course C1:

```
IS_ENROLLED_ON :=  
  IS_ENROLLED_ON  
  UNION  
  RELATION { TUPLE { StudentId SID ( 'S5' ),  
                    CourseId CID ( 'C1' ) } } ;
```

But that's not always convenient, and not easy for the system to do the update quickly, either.

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## INSERT, UPDATE, DELETE

The following shorthands are universally agreed on:

- **INSERT**, for adding tuples to a relvar
- **UPDATE**, for updating existing tuples in a relvar
- **DELETE**, for removing tuples from a relvar

loosely speaking!

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## INSERT

In **Tutorial D**:

**INSERT *relvar-name* *relation-expression* ;**

E.g.

```
INSERT IS_ENROLLED_ON  
  RELATION { TUPLE { StudentId SID ( 'S5' ),  
                    CourseId CID ( 'C1' ) },  
             TUPLE { StudentId SID ( 'S4' ),  
                    CourseId CID ( 'C4' ) } } ;
```

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## UPDATE

In **Tutorial D**:

**UPDATE *relvar-name* [ **WHERE** ... ] ( *attribute-updates* ) ;**

E.g.

```
UPDATE EXAM_MARK WHERE CourseId = CID ( 'C1' )  
  ( Mark := Mark + 5 ) ;
```

When it was decided that the exam for C1 had been a little too difficult, perhaps. Everybody who sat the exam gets 5 more marks.

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## DELETE

In **Tutorial D**:

```
DELETE relvar-name [ WHERE condition ] ;
```

E.g.

```
DELETE IS_CALLED WHERE Name = NAME ( 'Boris' ) ;
```

(Did we mean to do that? — there's more than one Boris!)

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## An Occasional Problem with Updating

Suppose the following constraints are in effect:

```
CONSTRAINT EnrolRecognisedStudentsOnly
IS_EMPTY (IS_ENROLLED_ON NOT MATCHING IS_CALLED);
```

```
CONSTRAINT RegisterEnrolledStudentsOnly
IS_EMPTY (IS_CALLED NOT MATCHING IS_ENROLLED_ON);
```

We can't enrol a student before we have named her and we can't name her before we have enrolled her on some course. *Impasse?*

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## Proposed Solution to The Impasse

“Multiple assignment”: updating several variables simultaneously.

In **Tutorial D**:

```
INSERT IS_CALLED
  RELATION { TUPLE { StudentId SID ( 'S6' ),
                     Name NAME ( 'Zoë' ) } } ,
INSERT IS_ENROLLED_ON
  RELATION { TUPLE { StudentId SID ( 'S6' ),
                     CourseId CID ( 'C1' ) } } ;
```

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## A Note on Multiple Assignment

Would the following have the same effect?

```
INSERT IS_CALLED
  RELATION { TUPLE { StudentId SID ( 'S6' ),
                     Name NAME ( 'Zoë' ) } } ,
INSERT IS_ENROLLED_ON
  EXTEND IS_CALLED WHERE Name = NAME ( 'Zoë' )
    ADD (CID('C1') AS CourseId) {StudentId, CourseId} ;
```

No! The second INSERT cannot see Zoë.

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